NUMERICAL ANALYSIS OF ELECTRO-HYDRAULIC FORMING PROCESS, BY USING VOLUMEACCELERATION LOADING

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ABSTRACT

Electro-hydraulic forming is one of the unique processes of high-velocity forming. In this process, the electrical energy is converted into the mechanical energy in the form of shock waves within a liquid medium. This energy is utilized to perform redundant work, to overcome the friction, and to form the work-piece to the final shape. This process is very similar to the explosive forming and the only difference is the source of energy. In this article, electrical discharge phenomenon was analyzed and the parameters involved in electro-hydraulic forming process were investigated. Then, the simulation of the process was performed using finite-element approach. In this research, three types of sheet metals were used which are mild steel (IF210), high strength steel (DPX800) and stainless steel (1.4509). In this simulation, a dynamic explicit analysis was adopted and the effect of electrical discharge was simulated both in the form of acoustic pressure loading and acoustic inward volume acceleration loading. Three-dimensional analysis was employed using a shell model as a sheet metal. The Johnson-Cook constitutive model was used to describe the plastic behavior of the material. Then, the geometry of the formed part and the strain distributions were evaluated.Finally, the results obtained from simulation were compared with the experimental results reported by other scientists and found a good correlation between them.

Keywords:*High velocity forming, Electro-hydraulic forming, Finite element method, Electrical discharge, Johnson-cook*
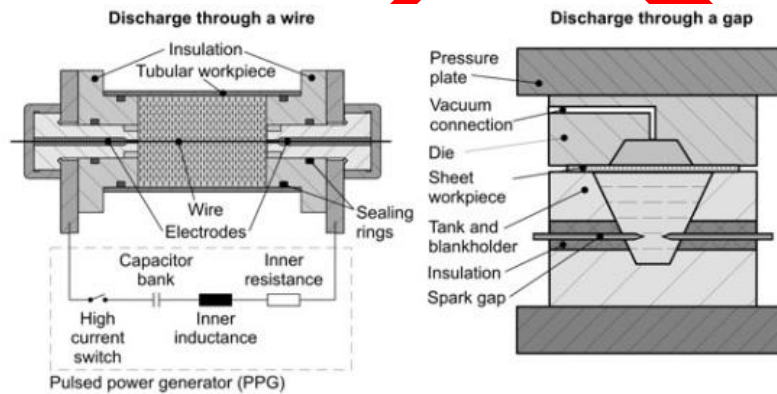
INTRODUCTION

   Electro-hydraulic forming is one of the methods that highly considered among automotive specialists. This method is known as "high strain rate forming" method. In this process, an electrical discharge within a liquid medium transforms the electrical energy into a mechanical energy. Figure 1, illustrates a schematic of this process. Severe discharge of electrical energy creates a plasma channel that leads to evaporation of the water between two electrodes and generates a high-speed shock wave

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propagating towards the work-piece. Thus, the sheet moves into the die cavity and reaches its desired shape. Carrying the force by the liquid medium, the need for a punch is revoked. Compared with electro-magnetic forming, this process can form versatile metals due to its non-sensitivity to conduction.

A capacitor bank is utilized to store the energy needed. If the work-piece being formed is large and its thickness is considerable, the use of larger bank is mandatory. Electro-hydraulic forming process lasts fewer than 200 micro-seconds and the forming velocity reaches to amount of 300 metre per second [1]. Equation (1), computes the amount of energy accumulated in a capacitor bank.

$$E_C = \frac{1}{2}CV^2$$
(1)

Where E_c is the energy stored in the capacitor (j), C is the electrical capacity (Farad), and V is the voltage difference (volt).

Fig. 1 schematic of electro-hydraulic machine

In 1940, EHF was recognized as a potential method for forming of various parts. Until 1953, there were no reports regarding the utilization of EHF method. Afterwards, Early and Dow reported an under-water electrical discharge to form a part [3]. In the early 1950s, preliminary developments were achieved by Yutkin [4]. Bruno [5], Davies and Austin [6] investigated the applications of the EHF approach. Balanethiram et al. [7] conducted a survey on EHF processes and the results showed an enhanced forming limit comparing to traditional processes.

Limited data are available on simulation of EHF processes. Simulations are mostly done by ABAQUS CAE, LS-DYNA, and CTH. Vohnout et al. investigated the non-homogenousity nature of the pressure in this process. Assuming the equivalency of electrical discharge with an explosive energy, they applied an explosion loading in CTH simulation software. The results confirmed the non-homogenousity of the pressure exerted to the work-piece.Golvashchenko et al. [2, 9] did many efforts regarding the simulation of the process in LS-DYNA. In terms of loading, instead of electrical discharge, the equation of state of the expansion gas was substituted. Melander et al. [10] applied dynamic explicit approach using ABAQUS CAE software and a pressure wave loading was adopted instead of electrical discharge. They evaluated the strain distribution and the final shape of the part.

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Finally a good correlation between simulations and experiments were obtained. Farzin and Montazerolghaem [11] also formed miniature products by EHF processes and by simulating in ABAQUS CAE, they investigated the effect of element size and time intervals in corner-filling of the die cavity.

SCOPE

In this article, due to the complex nature of the EHF process, electrical discharge, and its related parameters will be explained. Then, simulation of an EHF process for producing dome-shaped products using finite element approach will be developed. In terms of simulation, ABAQUS CAE dynamic explicit module will be utilized. Finally, the results from simulation will be compared with that of experiments and the correlation will be drawn between them.

ELECTRICAL DISCHARGE CIRCUIT

An electrical discharge circuit usually consists of a series of capacitors, keys, cables, and a discharge channel which has the electrical capacity of C, inductance of L, and resistance of R. figure 2, schematically illustrates a typical electrical discharge circuit. The capacitance is a lumped element, and inductance and resistance are distributed elements. Due to ignorable fluctuations, inductance of the circuit is considered constant. But as the equation 2 shows, the resistance of the circuit is divided into fix and variable parts.

$$R = R_o + R_d$$
(2)

Where R_o is the constant resistance and determines as:

$$R_o = R_i + R_c + R_s$$
(3)

Where R_i is the internal resistance of the capacitor, R_c is the resistance of the cables, R_s is the resistance of the keys, and R_d is the resistance of the discharge channel. In fact, the resistance level can decrease from kilo-ohm in the beginning of the process, to milli-ohm in the final stages of the discharge [12].
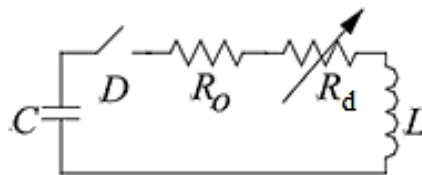

Fig. 2 schematic of discharge circuit in EHF

The current $i(t)$ in the electrical discharge circuit, can be determined by the differential equation as follows [13]:

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$$\frac{d^2 i}{dt^2} + \frac{R}{L}\frac{di}{dt} + \frac{1}{LC} i = 0$$

(4)

Considering the preliminary conditions of:

$$i(\circ) = \circ, \ \frac{di}{dt}\Big|_{t=\circ} = -\frac{V_\circ}{L}$$

And by solving the differential equation 4, current-time and voltage-time functions can be obtained [13]. Electrical power of the discharge channel is described as follows:

$$N(t) = i(t)V(t)$$

(5)

Where $i(t)$ and $V(t)$ are the current and voltage respectively. The energy released in the channel is determined as follows:

$$E_d(t) = \int_\circ^t N(t)dt$$

(6)

Where *t* is the duration of plasma phase in the channel. All the energy is not transferred into the channel and the wire and keys prevent the whole energy to discharge. Thus the circuit efficiency should be taken into account:

$$\eta_d = \frac{E_d}{E_C}$$

(7)

E_d is the energy of the channel and E_c is the energy stored in the capacitor bank.

ELECTRICAL DISCHARGE ENERGY

If the water is exposed to a high-voltage DC pulse, an avalanche of electrons will be generated nearby the anode and this leads the water to ionize. Electrons then accelerate towards cathode in the presence of the electrical field. So the plasma channel initiates. Temperature rises up to 10000 Kelvin [12]. By initiating the plasma channel, the water evaporates and expands quickly. This, creates shock waves.

Different types of energies will be generated in the discharging moment. These include internal energy, radiation energy, shock wave energy and the bubble energy [12].
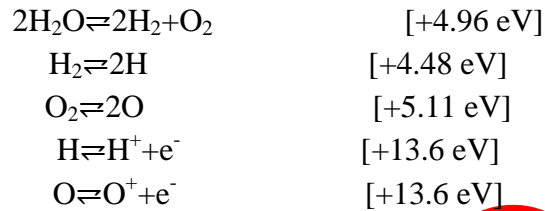
$$E_d = E_{in} + E_{ra} + E_s + E_b$$

(8)

E_{in}, E_{ra}, E_s and E_b are the internal energy, radiation energy, shock-wave energy and the bubble energy respectively.

INTERNAL ENERGY

The temperature in the plasma channel can reach up to 10000 Kelvin. At this temperature, the water evaporates and the steam behaves as an ideal gas with constant specific heat and dissolves to

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hydrogen and oxygen. According to Landau-lifshitz Law, a particle or ion within plasma channel can react in one of these 5 forms:

$$2H_2O \rightleftharpoons 2H_2 + O_2 \qquad [+4.96 \text{ eV}]$$
$$H_2 \rightleftharpoons 2H \qquad [+4.48 \text{ eV}]$$
$$O_2 \rightleftharpoons 2O \qquad [+5.11 \text{ eV}]$$
$$H \rightleftharpoons H^+ + e^- \qquad [+13.6 \text{ eV}]$$
$$O \rightleftharpoons O^+ + e^- \qquad [+13.6 \text{ eV}]$$

Information inside the bracket corresponds the minimum energy required to initiate reaction. Thus the energy added to the channel is determined by the equation 9:

$$E_{in} = \sum_i E_i$$
(9)

E_i is the energy added during each reaction.

RADIATION ENERGY

Thermal radiation depends on the temperature of the system and this phenomenon is described by Stefan-Boltzmann Law [12].

$$E_{ra} = 4\pi r_\circ^2 St$$
(10)

Where r_o is the radius of the channel, S is the electro-magnetic flux normal to channel area.

SHOCK-WAVE AND BUBBLE ENERGY

While electrical discharging beneath the water, shock-wave and bubble wave propagates through the medium. On account of the fact that the maximum pressure obtained from electrical discharge is reversely proportional with radial distance from the channel, the shock-wave energy is determined as follows:

$$E_s = 4\pi \int_0^\tau r^2 p(t) u(t) dt$$
(11)

Where u, the particle velocity is: $u(t) = \frac{p(t)}{c\rho}$. By substituting the u(t) in the equation above, the shock-wave energy can be determined as follows [12 and 14]:

$$E_s = \frac{4\pi \cdot r^2}{\rho c} \int_0^\tau p^2(t) dt$$
(12)

Where r is the distance from the source, ρ is the density of water, c is sound speed, τ is the width of shock-wave signal, and p(t) is the shock-wave pressure signal. The bubble wave energy is calculated by the equation 13 as follows:

$$E_b = \frac{4}{3}\pi p_m R_{mb}^3$$
(13)

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P_m is the maximum pressure, and the maximum bubble radius, R_{mb}, is calculated by:

$$R_{mb} = \frac{T_b}{1/84 \sqrt{\frac{\rho}{c}}}$$

(14)

T_b is the fluctuation period of the bubble.

SHOCK-WAVE PRESSURE

The experimental equation below computes the shock-wave pressure in different times [15]:

$$p(t) = p_m e^{\frac{-t}{\theta}}$$

(15)

$\boldsymbol{\theta}$ is the time constant and can be calculated as follows:

$$\theta = \frac{0/74 t_1 \overline{r}^{\frac{1}{8}}}{ln\,10} \; ; \; \overline{r} = r \times (\frac{\rho I_e}{V^2 C^2 L})^{\frac{1}{4}}$$

(16)

Where t_1 is the half-period of discharge and v, c and L are voltage, capacitor capacitance, and circuit inductance respectively and ρ is the density of the medium. On the other hand, the maximum Shockwave pressure is obtained by the equation 17 as follows [16]:

$$p(r) = p_{ch} r^{-0.5}$$

(17)

Internal energy of the channel is computed as follows [17]:

$$E_{pl} = \frac{p_{ch} V_{Ch}}{(\gamma - 1)}$$

(18)

Adiabatic coefficient depends on pressure temperature and the chemical composition of the plasma. In electro-hydraulic forming processes the adiabatic coefficient varies in small ranges.The pressure of plasma channel is calculated by equation 19 where $\rho_\circ$ is the preliminary density and ρ is the current density and E is the fracture energy.

$$P_{ch} = (\gamma - 1) \left(\frac{\rho}{\rho_\circ}\right) E$$

(19)

In electro-hydraulic forming processes there are many different parameters that we can divide them into 4 different categories:

DISCHARGING CIRCUIT

According to equation 1 discharging voltage is directly proportional to the energy stored in the capacitors. On the other hand, according to equation 7, the total energy stored in the capacitors does not discharge into the channel but some amount of this energy is wasted by the wires and keys. Equation 23 can be obtained regarding the equations 20 and 21:

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$$\beta = \frac{R}{2}\sqrt{\frac{C}{L}}$$
(20)

$$t_c = \sqrt{LC}$$
(21)

Where L is the inductance of the circuit, C is the capacitor, V_o is the preliminary voltage, h is the stand-off distance and Q is the Spark parameter. If the wire is used between the electrodes, the efficiency of the system will be enhanced and this leads to better control of the discharging path [24]. The wire parameters include: material, wire diameter, length, form and inductance of the wire. The material can be copper or aluminum. If the energy is less than 100 jule per centimeter, it is recommended to use aluminum wire but if the energy increases, its efficiency drops and the use of copper will be helpful [14]. If the energy is extremely high, utilizing thicker wires is recommended [25].

Electrodes stand-off distance, due to its acoustic impedance, play a vital role in applied pressure on workpiece. According to the results from [19], increasing the distance, exponentially reduces the shockwave pressure applied on workpiece. Stand-off distance shall not be smaller than electrodes gap. This is to prevent the creation of arcs. On the other hand, this distance should not exceed its standard amount to avoid the pressure loss on the workpiece.

MEDIUM

Some of the parameters in selecting the medium should be taken into account. These are: specific resistance, latent heat of evaporation, and acoustic impedance. In addition to medium properties, some other factors are also impact the plasma channel. These factors are: impurity of the medium, volume of the medium and preliminary pressure. Increasing the volume of the channel, reduces the electrical resistance of the medium [22].

According to the literatures, the most common mediums include: water, oil, and air. Woetzel et al [24] investigated three different types of mediums (water, oil, and air) and the result showed that water was the best and oil was the worst mediums respectively.

CAVITY

An utmost affair should be considered in terms of the design of the cavity. Cavity should withstand the dynamic pressure produced by prompt discharge of the capacitors. The volume of the cavity has to be designed properly to obtain the most efficiency. Increasing the volume results in shockwave attenuation. Moreover, the inside geometry of the cavity impacts the shockwave reflection resulting in better forming of the material [26].

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MODEL

The model consists of three parts: blank, die and water. Five different sheet materials are formed experimentally by other researchers. The simulation will be carried out and will be verified with the results of the experiments. The diameter of the hole in the die is 165 millimeters, the blank diameter was 175 millimeters which represent the diameter of the locking barb in the die. The die is a solid material with a truncated cone shape. The blank is shaped within the die. In the simulation, the blank is free formed and gets a free expansion, i.e. the die role is to restrict the diameter of the dome. The die consists a rounded edge with a radius of 4 millimeters for the blank to get bend over.

PROPERTIES

The input properties of the blank were given to the software ABAQUS. Its density set to 7800 [kg/m3], Young's modulus 210 GPa and the Poisson's ratio 0.3 [7]. For all the grades, these properties were constant. For demonstrating of the plastic behavior of the sheet, a Johnson-Cook constitutive model was used. For the materials in this research, JC material model parameters were obtained by the experiments done by other researchers [10]. The blanks are modelled as a shell element and have 5 integration points in thickness. The shell thickness in the simulation is set to the corresponding thickness of the experiment.

$$\bar{\sigma} = [A + B\bar{\varepsilon}^n]\left[1 + CLn\left(\frac{\dot{\bar{\varepsilon}}}{\dot{\varepsilon}_0}\right)\right]\left[1 - \left(\frac{T-T_\circ}{T_m-T_\circ}\right)^m\right]$$

(18)

In JC constitutive model $\bar{\sigma}$ is the flow stress. Three brackets can be seen in the equation. The first bracket represents the initial yielding strength and the strength hardening due to stain, where *A* is the initial strength and *B* and *n* are the representatives of the hardening due to strain (*ε*). The second part expresses the hardening due to strain rate, where *C* is the hardening sensitivity due to strain rate $\dot{\bar{\varepsilon}}$ and $\dot{\varepsilon}_0$ is a normalizing strain rate reference. The last section of the equation shows the material softening. Material heating correspond with the parameter *T*. T_o and T_m represent the initial temperature and the melting temperature respectively and they remain constant. In this paper, the impact of the temperature was ignored and the parameter *T,* was not evaluated.

Table 1 Johnson-cook parameters for the sheet metals [10]

Material	A(MPa)	B(MPa)	C	n	$\dot{\varepsilon}_0$
IF210	300	344	0.03	0.53	0.01
DPX800	698	970	0.01	0.52	0.01
1.4509	372	571	0.03	0.61	0.01

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INTERACTION

A friction coefficient of 0.1 in penalty was considered between die and blank. Also a surface to surface condition was considered as contact interaction, with contact property tangential behavior. The contact interaction between water and the blank was a tie constraint, with the blank as the master surface and the water as the slave surface. The water was given an acoustic impedance on the surface. The impedance determines the border to the EHF chamber. A non-reflecting sphere with a radius of 0.1 meter was applied as the condition on the water.

CONSTRAINTS

The blank is constrained with an encastre condition i.e. locked on all its 6 degree of freedom, on the border that represent the same diameter as the die has the locking barb in the EHF die. Figure 4 shows theboundary conditions in EHF simulation. The die is constrained on its reference point with an encastre condition.On the surface that borders to the EHF chamber, the water is constrained with an encastre condition.

Fig. 3 Boundary conditions in EHF simulation

LOAD

In the EHF process, the arc is generated in the back of the chamber. In the simulation, an acoustic inward volume acceleration positioned on the center of the back surface of the water as a substitution for arc. A Cosine-curve with amplitude of 1 and a length of 100 μ_s represents this pulse [1, 10], See Figure 6. The pulse shape does not have a significant impact on dome height and the strain distribution. Only the force under the curve controls the forming degree of the dome.

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Fig. 4 Acoustic Acceleration pulse model [1]

The relation between the input energy in the experiment and the input volume acceleration in the simulation should be obtained correctly. But the relation is complex and creating this relation is a tough job. For this purpose, for grade IF210, a reference magnitude of the pulse is set, so that the height of the formed blank in simulation and the height of the dome in the EHF experiment reach the same amount. For determination of the volume acceleration for other grades, the reference magnitude is recounted regarding to the respective input energy in the experiment. According to the Equation 11, the magnitude of grades (the acceleration) correspond with the square of the change relative to the reference magnitude. In Equation 11, E is the energy, q is the changing fraction of the input energy, and p is the changing fraction of the acceleration.

ELEMENT TYPE AND MESH FOR BLANK

A 3D deformable shell chose for the blank. Element type S4R; a 4-node doubly curved thin or thick shell, reduced integration, hourglass control, finite membrane strains.A quadratic mesh with a global seeding of 3 millimeters was applied. On the edge of the blank, much more refined seeding of 0.5 millimeters in the radius direction was considered. This mesh size was mandatory to determine the rounded edge on the die, and a smooth strain distribution.

Fig. 5 Sheet mesh pattern

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ELEMENT TYPE AND MESH FOR WATER

A 3D deformable solid was considered for the water. Element type AC3D8R was applied for the water: This element is an 8-node linear acoustic brick, reduced integration, hourglass control. The element is a hexagonal acoustic type with a seeding of 50 elements on one base diameter (4 millimeters) and element height of 13 millimeters.

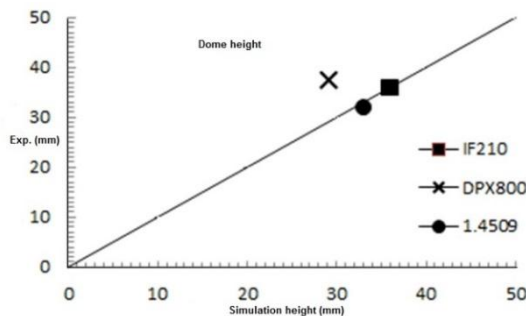**Fig. 6** Sheet mesh pattern

Rigid body, die

The die is modelled as a 3D analytical rigid shell and does not need any mesh.

RESULTS AND CONCLUSION

The dome heights are shown in figures 8. The reference grade is IF210. All other magnitudes (grades) are based on IF210. These grades are recalculated through both Equation 11 and the input energy from the experiment.

Fig. 7 Deformed sheet simulated by inward volume acceleration loading, for IF210

Fig. 8 Deformed sheet simulated by inward volume acceleration loading, for IF210

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